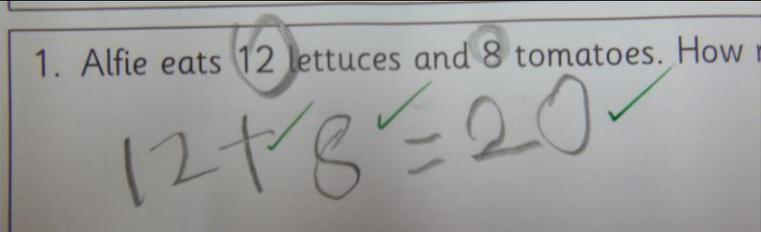
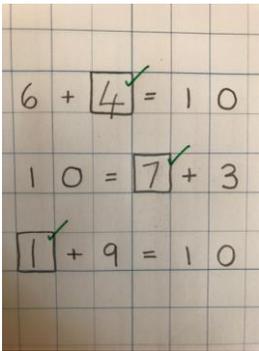
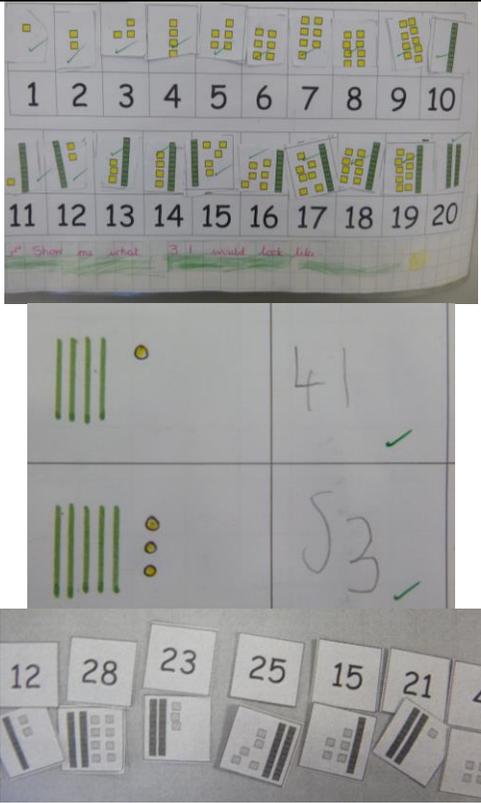
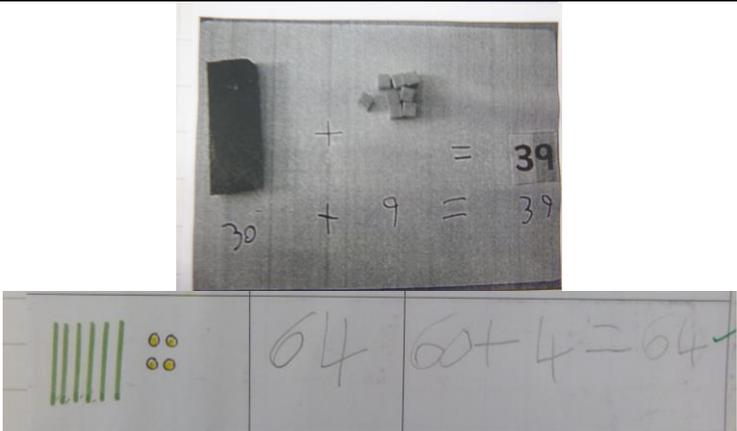
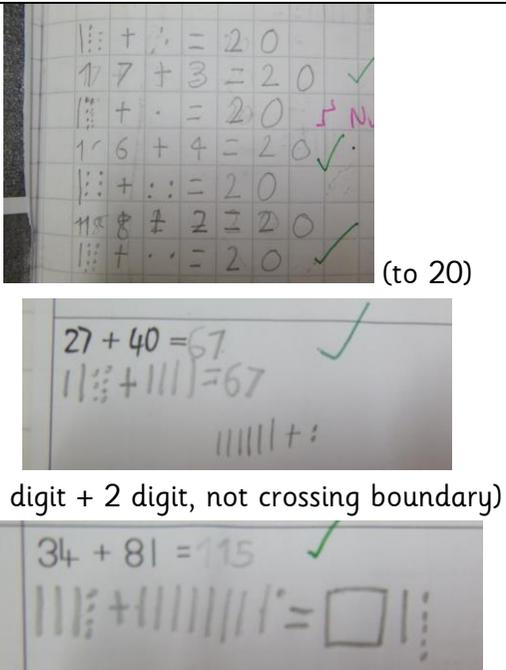
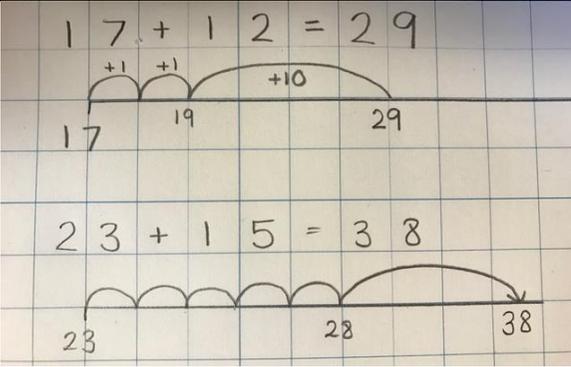
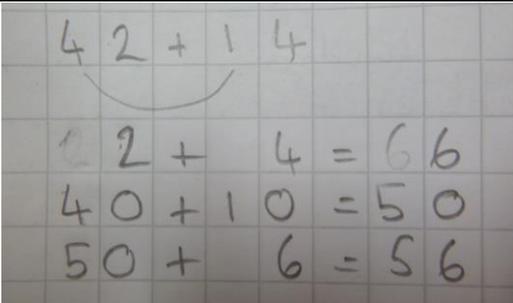
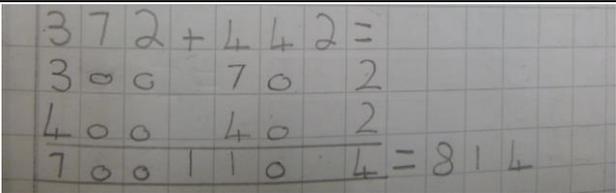
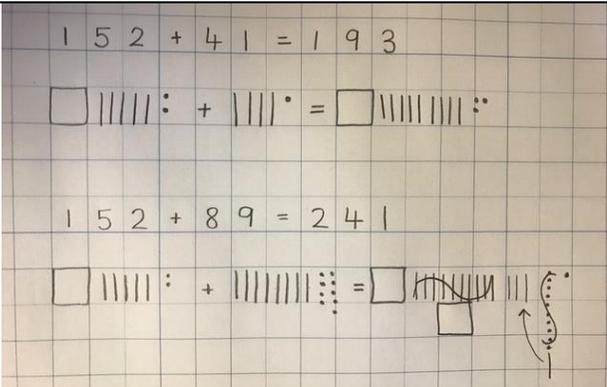


# Addition

	Focus	Example	Notes
1	<b>Immersion in numbers and combining numbers to make totals</b>		Children are immersed in numbers and counting throughout the Foundation Stage.
2	<b>Use of manipulatives to make totals (informal)</b>		Children should progress through counting cubes, straws, objects etc.  Children should then be introduced to a bundle of 10 straw; making 10 (before Dienes)
3	<b>Recording of linear number sentences using + and = symbols</b>		One number per square

<p><b>4</b></p>	<p><b>Linear number sentences with missing numbers</b></p>		<p>= symbol should be learnt as a 'balance' and be placed at either end of the number sentence e.g. <math>2 + 8 = 10</math> and <math>10 = 2 + 8</math></p>
<p><b>5</b></p>	<p><b>Introduction to Dienes to show the partition of numbers</b></p>		<p>Children should begin to appreciate the relative size of tens and ones and recognise 2 digit numbers as being made from tens and ones (TO)</p>

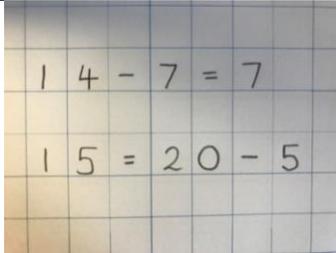
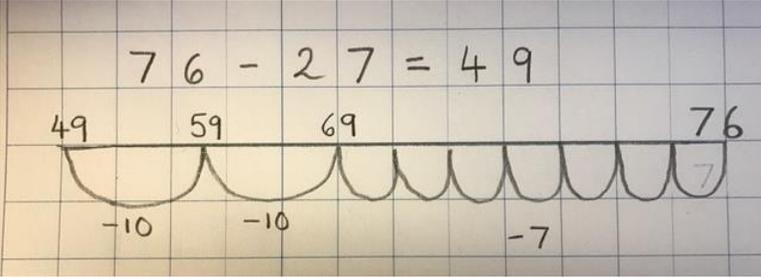
<p><b>6</b></p>	<p><b>Use of manipulatives to make totals (Dienes)</b></p>		<p>Children should move through using manipulatives to informal jottings.</p>
<p><b>7</b></p>	<p><b>Addition using Dienes to create informal jottings</b></p>	 <p>(to 20)</p> <p>(2 digit + 2 digit, crossing 100 boundary)</p>	<p>Jottings should be uniform in size.</p> <p>□ = hundred</p> <p>  = ten</p> <p>• = one</p>

8	Number line		<p>(NB: number lines and Dienes are to be offered for children in any order. Once taught, children will then have the opportunity to use the method they choose)</p> <p>Children should add ones first and then tens. This ensures consistency when progressing to the column methods.</p> <p>'Jumps' go above the number line and numbers go below (opposite in subtraction on a number line).</p>
9	Expanded Addition		<p>Children begin by partition the number HTO/TO</p> <p>Children then show the linear number sentences for each of the partition, beginning with the ones.</p>
10	Expanded Column		<p>Children expand each number by partitioning the number into HTO/TO</p> <p>Each partition is written in columns, stacked above/below its corresponding HTO from the other number to be added.</p> <p>Beginning with then ones, each column is added. Totals for each of the HTO columns are combined mentally to make the final total.</p>
11	Expanded Column (with Dienes)		<p>This may be used before the written method to illustrate how ones and ten are exchanged; as a visual representation of why numbers are 'carried'.</p>

<p>12</p>	<p><b>Compact Column</b></p>	<div data-bbox="622 97 1093 357" data-label="Equation-Block"> </div> <p>(2 digit + 2 digit without and with exchange)</p> <div data-bbox="607 437 1111 671" data-label="Equation-Block"> </div> <p>(3 digit + 3 digit without and with exchange)</p> <div data-bbox="719 748 999 975" data-label="Equation-Block"> </div> <p>(4 digit + 4 digit with exchange)</p>	<p>Presentation policy should be reinforced here to ensure that the corresponding columns are stacked correctly in each of the numbers to add.</p> <p>Once taught addition without exchange, children should then apply this to numbers of varying size.</p>
<p>13</p>	<p><b>Compact Column</b> <b>(with decimals)</b></p>	<div data-bbox="651 1075 1064 1406" data-label="Equation-Block"> </div> <p>(decimal + decimal with exchange)</p>	<p>Decimal points should always be in-line.</p>



# Subtraction

	Focus	Example	Notes
1	Number sentences		<p>Basic reinforcement of beginning at the starting number and then counting back using a number line, and then mentally to find the total.</p> <p>Number sentences should be represented in reverse as well, using the = symbol as a 'balance'.</p>
2	Number lines (partitioning)		<p>Empty number line provided, progress to children drawing the empty number line.</p> <p>Starting number written at the right end of number line.</p> <p>Partition second number and subtract the ones first and then the tens.</p> <p>'Jumps' go below the number line and numbers go above (opposite in addition on a number line).</p>

<p><b>3</b></p>	<p><b>Using Dienes to create informal jottings</b></p>	<div data-bbox="651 204 1077 437" data-label="Image"> </div> <p>(2digit – 2 digit without decomposition)</p> <div data-bbox="667 533 1064 863" data-label="Image"> </div> <p>(2digit – 2 digit with decomposition)</p>	<p>These replicate the jottings used when adding with jottings (see above)</p> <p>Children create the starting number using jottings for tens and ones. Children then cross out the ones and tens being subtracted and then add the remaining total to find the answer.</p> <p>Decomposition is required when the value in the ones column is higher in the number being subtracted, than in the starting number.</p> <p>A S drawn over the ten being exchanged is used to show that decomposition has taken place.</p>
<p><b>4</b></p>	<p><b>Number lines</b> (counting on to find the difference between close numbers)</p>	<div data-bbox="488 1023 1245 1350" data-label="Figure"> </div>	<p>When the target number is a multiple of 10 (Change from £1 when you've spent 76p): Add ones to reach the next multiple of ten (80p) and then tens to reach the target (100p)</p> <p>When the target number is not a multiple of ten (the difference between 87 and 35): Add ones to until the value in the ones column matches that of the target number.</p>

5

## Expanded Column

$$\begin{array}{r} 56 - 25 = 31 \\ \underline{50} \quad \quad 6 \\ \underline{20} \quad \quad 5 \\ 30 \quad \quad 1 \end{array}$$

(2 digit – 2 digit without decomposition)

$$\begin{array}{r} 62 - 38 = 24 \\ \begin{array}{r} 50 \\ \cancel{60} \end{array} \quad \quad \begin{array}{r} 12 \\ \underline{8} \end{array} \\ \underline{30} \quad \quad 8 \\ \underline{20} \quad \quad 4 \end{array}$$

(2 digit – 2 digit with decomposition)

$$\begin{array}{r} 3865 - 253 = 612 \\ \underline{800} \quad \underline{60} \quad \underline{5} \\ \underline{200} \quad \underline{50} \quad \underline{3} \\ 600 \quad 10 \quad 2 \end{array}$$

(3 digit- 3 digit without decomposition)

$$\begin{array}{r} 752 - 314 = 438 \\ \begin{array}{r} 40 \\ \cancel{700} \end{array} \quad \begin{array}{r} 12 \\ \underline{50} \end{array} \\ \underline{300} \quad \underline{10} \quad \underline{4} \\ \underline{400} \quad \underline{30} \quad \underline{8} \end{array}$$

(3 digit – 3 digit with decomposition)

Numbers are partitioned into TO or HTO and set out in a columns.  
Subtraction begins with the ones.

6

Compact Column

$$\begin{array}{r} 58 \\ - 24 \\ \hline 34 \end{array}$$

(2 digit – 2 digit without decomposition)

$$\begin{array}{r} 78 \\ - 37 \\ \hline 44 \end{array}$$

(2 digit – 2 digit with decomposition)

Apply

$$\begin{array}{r} 1. \ 596 \\ - 422 \\ \hline 174 \checkmark \end{array}$$
$$\begin{array}{r} 2. \ 8752 \\ - 543 \\ \hline 332 \checkmark \end{array}$$

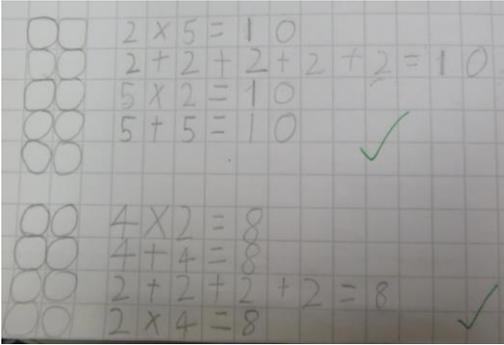
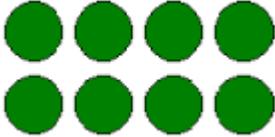
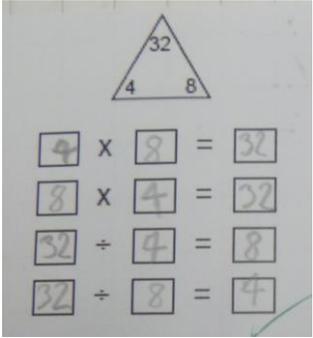
(3 digit – 3 digit without decomposition)

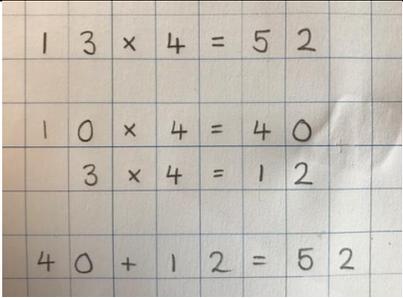
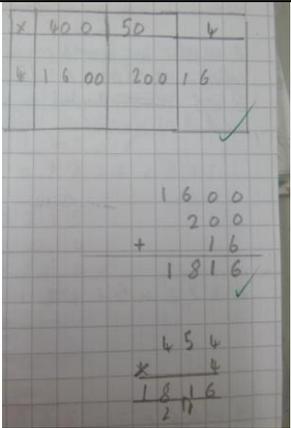
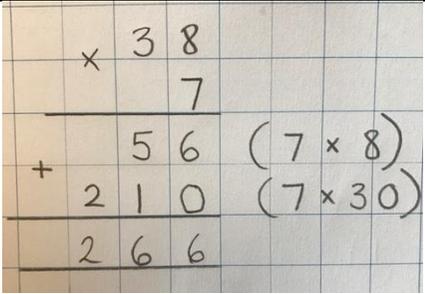
$$\begin{array}{r} 1812 \\ - 157 \\ \hline 055 \end{array}$$

(3 digit – 3 digit with decomposition)

Presentation reflects that used in addition.

# Multiplication

	Focus	Example	Notes
1	x table facts		<p>There is an expectation that children will learn, by heart, the following multiplication tables...and be able to link this to solving division facts.</p> <p><b>Year 2:</b> x2 x5 x10  <b>Year 3:</b> x3 x4 x8  <b>Year 4:</b> x6 x7 x9</p>
2	Arrays- counting in groups/repeated addition		<p>Children should appreciate that an array represents 2 multiplication facts.</p> <p>E.g.</p>  <p>4 x 2    and    2 x 4</p> <p>Arrays should also be linked to repeated addition facts.</p>
3	Fact Families		<p>These can be used to show the relationship between multiplication and division.</p>

4	<b>Linear Partitioning</b>		This method requires children to have secure multiplication fact recall.
5	<b>Expanded Grid</b>	 <p>(3 digit x 1 digit)</p>	This method relies on the children having secure place value knowledge (e.g. $4 \times 4 = 16$ , so $400 \times 4 = 1600$ )
6	<b>Vertical Column Expanded</b>		This method supports the learning of the vertical column compact method as encouraged children to making annotations of the multiplication facts that they are solving to arrive at the final answer.

7

**Vertical Column  
Compact**

A handwritten vertical multiplication problem on a grid. The multiplicand is 108 and the multiplier is 9. The product is 972. The digits are written in a compact vertical column format.

(3d x 1d)

Two handwritten vertical multiplication problems on a grid. The first is 25 multiplied by 50, resulting in 1250. The second is 1250 multiplied by 20, resulting in 25000. The digits are written in a compact vertical column format.

(2d x 2d and 4d x 2d)

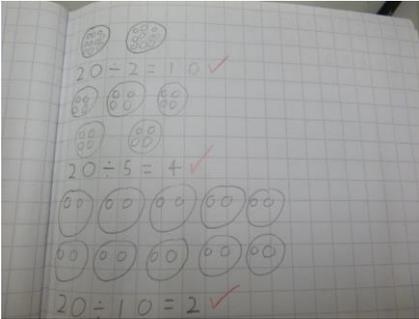
Two handwritten vertical multiplication problems on a grid. The first is 15 multiplied by 32, resulting in 480. The second is 480 multiplied by 40, resulting in 19200. The digits are written in a compact vertical column format.

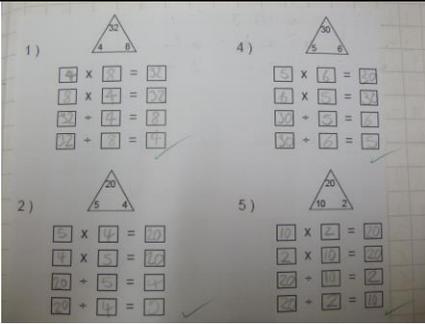
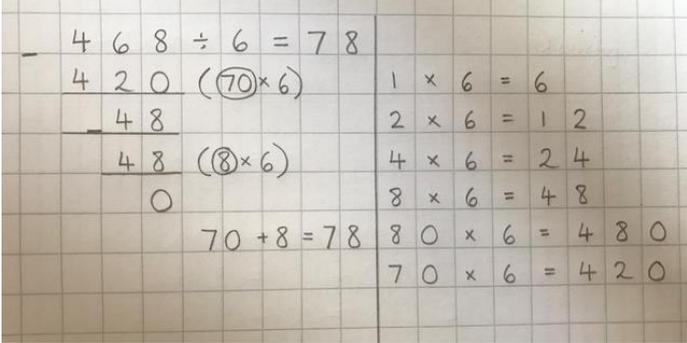
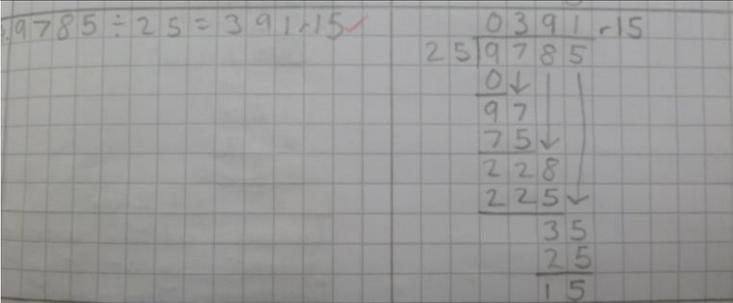
(2d x 2d and 3d x 2d)

This is the method that all children will arrive at.

This method combines many aspects of the previous methods, but is compact.

# Division

	Focus	Example	Notes
1	Practical Sharing		
2	Sharing and Grouping	 <p>(Sharing)</p>	<p>Both sharing and grouping are important. Both can be shown visually...</p> <p><b>Grouping</b> - when the <b>number being shared</b> and the <b>group size</b> is already known, but number of groups is unknown E.g. How many groups will we have if we split our class of 30 into groups of 5? Children will create full groups of 5 until they reach their target of 30.</p>  <p><math>30 \div 6 = 5</math></p> <p><b>Sharing</b> - when the <b>number being shared</b> and the <b>number of groups</b> are already determined, but the group size is unknown. E.g. I need to split the class of 30 children into 5 equal groups. How many children will be in each group? Children would create the 5 empty groups and then share out members equally until they reach 30.</p>  <p><math>30 \div 5 = 6</math></p>

<p><b>3</b></p>	<p><b>Fact Families</b></p>	 <p>1) Triangle with 12 at top, 4 and 3 at bottom. Equations: <math>4 \times 3 = 12</math>, <math>3 \times 4 = 12</math>, <math>12 \div 4 = 3</math>, <math>12 \div 3 = 4</math>.</p> <p>2) Triangle with 20 at top, 5 and 4 at bottom. Equations: <math>5 \times 4 = 20</math>, <math>4 \times 5 = 20</math>, <math>20 \div 5 = 4</math>, <math>20 \div 4 = 5</math>.</p> <p>3) Triangle with 30 at top, 5 and 6 at bottom. Equations: <math>5 \times 6 = 30</math>, <math>6 \times 5 = 30</math>, <math>30 \div 5 = 6</math>, <math>30 \div 6 = 5</math>.</p> <p>4) Triangle with 20 at top, 10 and 2 at bottom. Equations: <math>10 \times 2 = 20</math>, <math>2 \times 10 = 20</math>, <math>20 \div 10 = 2</math>, <math>20 \div 2 = 10</math>.</p>	<p>These can be used to show the relationship between multiplication and division (and other inverse operations)</p>
<p><b>4</b></p>	<p><b>Short Division Chunking</b></p>	 <p>Handwritten work on grid paper showing the division <math>468 \div 6 = 78</math> using chunking. The student identifies chunks: <math>70 \times 6 = 420</math> and <math>8 \times 6 = 48</math>, which sum to <math>70 + 8 = 78</math>. A multiplication table for 6 is also shown.</p> <p>(3 digit <math>\div</math> 1 digit)</p>	<p>Relies on children being fluent in all multiplication facts. Children create 'chunks' of multiples to take away from the starting number until they get to 0. In this case, the 6 times table has allowed the child to create a variety of 'chunks' and this has been subtracted using column method.</p>
<p><b>5</b></p>	<p><b>Long Division</b></p>	 <p>Handwritten long division of <math>9785 \div 25 = 391 \text{ r } 15</math>. The student shows the steps of dividing 97 by 25 to get 3, then 978 by 25 to get 39, and finally 9785 by 25 to get 391 with a remainder of 15.</p> <p>(4 digit <math>\div</math> 2 digit with remainder)</p>	<p>This method prepares children for Short Division. It allows them to see the maths that is happening in the 'Short' method. Long division can have a remainder expressed as a decimal.</p>

**6 Short Division**

$$34 \div 2 = 17$$
$$\begin{array}{r} 17 \\ 2 \overline{)34} \end{array}$$

Simple Short Division- Without remainders

$$\begin{array}{r} 046 \text{ r}7 \\ 8 \overline{)375} \end{array}$$

Simple Short Division- With remainders

$$\begin{array}{r} 0314.2 \\ 25 \overline{)785.50} \end{array}$$

Short Division 4 digit  $\div$  2 digit with decimal remainder

Known as the 'bus stop method'. Number being divided is written inside the 'bus stop'.